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THESIS

DESIGN OF A MATCHING NETWORK FOR DIPOLE ANTENNAS

by

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March 1993

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Design of a Matching Network for Dipole Antennas

by

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Lieutenant, United States Navy
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ABSTRACT

The input impedance of an antenna is highly dependent on the frequency range in which it operates. For an electrically small antenna to operate in a broad frequency range, the antenna must be properly matched. This thesis presents the design of a matching network for a 1-meter monopole antenna, operating over 30-90 MHz using the real frequency method (RFM). It outlines the mathematical steps needed to determine the equalizer function, which ultimately leads to the circuit design. The goal of the RFM, given the real frequency data, is to optimize the Transducer Power Gain (TPG), and minimize the reflection coefficient or power lost due to the impedance mismatch. A complete design including network realization is given. However, no experimental results are presented.

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I. INTRODUCTION

One of the important factors in antenna performance is the input impedance. The antenna impedance consists of both real (resistance) and imaginary (reactance) parts. The reactive component is generally unwanted because it gives rise to stored energy in the near field of the antenna [Ref. 8].

The input impedance is primarily determined by the geometry and electrical size of the antenna, and it can be significantly different from the impedance of the generator. To optimize the power transfer from the generator to the antenna, it is necessary to insert an impedance transformer between the two. Ideally, the transformer (or matching network) should be designed to eliminate the reactive component of the antenna impedance, and at the same time provide an input resistance equal to that of the generator. This is relatively easy to accomplish at a single frequency, but becomes more difficult as the operating frequency of the antenna increases.

Until the development of the real frequency method (RFM), a broadband matching network had been designed by an analytic method or by an iterative trial and error procedure. An analytic method requires complex and rigorous mathematics even for a simple network. However, RFM, developed by Carlin in 1977, made designing a matching network simpler, more direct

and less complex. It does not assume an equalizer topology, nor does it require an analytic description of the load (input impedance of the antenna in our case) as long as it can be obtained by some means [Ref. 1]. It is a numerical method that only requires the real frequency data of the load for the frequency band of interest [Ref. 1].

Although several approaches have been published for broadband impedance matching, none has been tailored specially for broadband monopole antennas. However, in his recent work, Rao [Ref. 10] has built and tested a matching network for a loaded monopole antenna at HF using the resistivity profile developed by Wu and King [Ref. 11]. Unfortunately, that antenna is 35 feet long and is not an acceptable candidate for manpack or vehicular mount. Therefore a 1-meter monopole antenna was chosen. Like a dipole, this antenna is narrow band and it is "electrically small" in the very high frequency (VHF) band. However, it can be made broadband by resistive loading and properly designing a matching network.

This thesis describes the mathematical basis of RFM and uses this approach to design a matching network for a 1-meter monopole antenna operating over 30-90 MHz.

II. MATHEMATICAL BASIS FOR RFM

In this chapter, the basic concept of RFM is described and the steps for implementing the RFM are outlined.

A. CONCEPT OF RFM

The best way to describe the concept of a matching network or equalizer circuit is through the simple description of a lossless two port network (Figure 1). In a two port network, we are interested in relating current and voltage at one port to current and voltage at the second port. This gives us a transfer function that characterizes the relationship between the two ports.

One of the design requirements of broadband matching is to maximize power transfer between a power generator and the load over a given frequency range. To this end we consider the transducer power gain (TPG) as defined by Carlin [Ref. 1]

$$TPG = T(\omega) = \frac{Power\ Delivered\ to\ Load}{Power\ Available\ from\ the\ Generator} = 1 - |\rho^2|$$

where p is the complex reflection coefficient,

$$\rho = \frac{Z_q - Z_L^*}{Z_q + Z_L}$$

between the equalizer and the load.

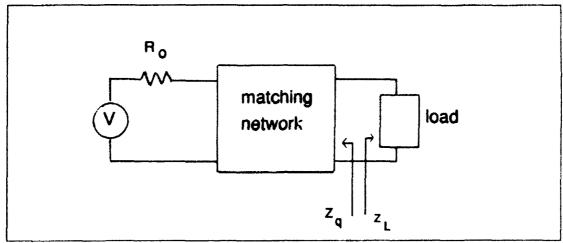


Figure 1 Simple Two-port Network

It can be seen from the previous equation that a perfectly matched network will have a gain of one. However, this is an unrealistic design that is not achievable in practice. goal is to design a network which minimizes ρ and maximizes the power delivered to the load.

For a given load impedance, looking at the Thevenin equivalent circuit from the loaded port [Ref. 1] allows us to find an equalizer impedance, $Z_q(\omega)$. Expressing the TPG in terms of load impedance and equalizer impedance,

$$T(\mathbf{\omega}) = \frac{4R_L(\mathbf{\omega})R_q(\mathbf{\omega})}{|Z_L(\mathbf{\omega}) + Z_q(\mathbf{\omega})|^2}$$
(1)

where

 $R_{t}(\omega) = load resistance$

 $R_a(\omega)$ = equalizer resistance

 $Z_L(\omega)$ = load impedance $Z_q(\omega)$ = equalizer impedance.

B. MATHEMATICAL DEVELOPMENT

The fundamental approach of RFM is its use of real frequency data to determine an equalizer function. In general, the impedance of the network can be complex: $Z_q(\omega) = R_q(\omega) + j X_q(\omega), \text{ where } R_q(\omega) \text{ is the real part and } X_q(\omega) \text{ is the imaginary part. We will use } R_q(\omega) \text{ to find } Z_q(\omega). \text{ The key, of course, is finding the real part. In a step-by-step procedure, the next two sections are devoted to finding the real part (resistance) of the complex impedance function, and the following section derives the equalizer impedance. One thing to note is that the poles of the equalizer impedance must be in the negative half (left) of the complex frequency plane.$

1. Linear Combination Approximation

It is desired to design a broadband equalizer in the frequency range $\omega_L < \omega < \omega_H$. The given frequency range is first partitioned into smaller bands, and the resistance is assumed to behave linearly within each sub-band. Several out-of-band break points are added from zero frequency to the lower frequency ω_L , and one frequency break point, ω_h , is added beyond ω_H . The choice of ω_L depends on the roll-off desired.

The first step in solving for an equalizer impedance is to obtain a linear approximation of the resistance, $R_q(\omega)$. The values of $R_q(\omega)$ are dependent on the excursive resistances, r_k , or the unknowns. The excursive resistances are the ramp values between each of the break points,

 $0<\omega<\omega$. . .< ω , for a given frequency range [Ref. 7]. The number of unknowns are determined by the break points. For example, if there are n break points, there are n-1 unknowns. The relationship between R (ω) and r is [Ref. 1]

$$R_q(\omega) = r_o + \sum_{k=1}^{N} a_k(\omega) r_k$$
 (2)

where

$$a_{k}(\omega) = \frac{\omega - \omega_{k-1}}{\omega_{k} - \omega_{k-1}}, \qquad \omega_{k-1} < \omega < \omega_{k}$$

$$0, \qquad \omega < \omega_{k-1}$$
(3)

and r = DC resistance.

The equalizer resistance, $R_3(\omega)$, is made zero for $\omega > \omega$, [Ref. 1]. From equations (2) and (3), this means that

$$r_o = -\sum_{k=1}^n r_k. \tag{4}$$

If the DC resistance value r is available, the number of unknowns is no longer n-1 but n-2, and we have

$$r_n = -(r_o + \sum_{k=1}^{n-1} r_k). {(5)}$$

We have only considered the real frequency data thus far. However, an equalizer impedance function has both even (real) and odd (imaginary) parts. Since the resistance is assumed to be piecewise linear in frequency, the reactance will be defined in the same manner [Ref. 1]. As in the case

of the resistance, the reactance is expressed in terms of the excursive resistances

$$X_{Q}(\omega) = \sum_{k=1}^{N} b_{k}(\omega) r_{k}$$
 (6)

where the coefficients b are obtained from [Ref. 3]

$$b_{k}(\omega) = \frac{1}{\pi (\omega_{k} - \omega_{k-1})} \int_{\omega_{k-1}}^{\omega_{k}} \ln \left| \frac{y + \omega}{y - \omega} \right| dy.$$
 (7)

They can be written in a closed form [Ref. 4] as

$$b_k(\omega) = \frac{1}{(\omega_k - \omega_{k+1})} \omega_k[(x+1)\log(x+1) + (x-1)\log|(x-1)| - 2\log(x)]$$

where

$$x = \frac{x_i}{x_k}.$$

With the real and imaginary parts defined, an IMSL optimization routine ZXSSQ can be employed to find the excursive resistances required to produce a given TPG. The error function to minimize is $|T-T(\omega)|$, where T is the assumed power gain, which can be increased until the resistance values just begin to become negative.

2. Rational Approximation

The second step is to obtain a rational function which closely approximates the piecewise linear curve specified by the resistive excursions [Ref. 2]. This is done so that a circuit realization of the equalizer impedance can be determined using the Gewertz method which requires a ratio of

polynomials. For convenience, we assume that the DC resistance, \mathbf{r}_{\circ} , is zero in the subsequent development.

Previously we have stated that $R_q(\omega)$ must be non-negative for an infinite frequency range [Ref. 1]. This places a constraint on an optimization routine, and constrained optimization is difficult to handle. This is because most optimization routines are written for unconstrained conditions [Ref. 5].

Direct use of the unconstrained optimization will lead to positive and negative values of resistances which are unacceptable. To get around this, the numerator and denominator polynomials in the rational function approximation

$$\hat{R}_{q}(\omega) = \frac{(A_{o} + A_{1}\omega^{2} + \ldots + A_{m}\omega^{2m})}{(1 + B_{1}\omega^{2} + \ldots + B_{n}\omega^{2n})} = \frac{A(\omega^{2})}{B(\omega^{2})}$$

are expressed in terms of a second polynomial of the form, $P_n(\omega) = 1 + x_1\omega + \ldots + x_n\omega^n.$ The denominator polynomial, for example, can be written as

$$B(\omega^{2}) = \frac{1}{2} \left[P_{n}^{2}(\omega) + P_{n}^{2}(-\omega) \right]. \tag{9}$$

Noting that $R_q(0)\!=\!0$ and using only one term in the numerator polynomial, the rational resistive function can now be written as

$$\hat{R}_{q}(\omega) = \frac{x_{o}^{2}\omega^{2k}}{B(\omega^{2})} = \frac{A_{1}\omega^{2}}{1 + \sum_{n=1}^{N} B_{n}\omega^{2n}},$$
(10)

where the coefficients A_1 and B_n in terms of x_i are as follows [Ref. 5]:

$$A_{1} = x_{0}^{2} \succ 0$$

$$B_{1} = x_{1}^{2} + 2x_{2}$$

$$\vdots$$

$$\vdots$$

$$B_{k} = x_{k}^{2} + 2 (x_{2k} + \sum_{j=2}^{k} x_{j-1} x_{2k-j+1})$$

$$B_{n} = x_{n}^{2} \succ 0$$
(11)

Although the x_i 's may be negative, $\hat{R}_q(\omega)$ is greater than zero in view of equation (9). Again, the IMSL optimization routine ZXSSQ can be employed to find the x_i coefficients. The function to minimize is $|\hat{R}_q - R_q|$.

3. Equalizer Impedance Using Gewertz Method

With the real part of equalizer approximated as a rational function, Gewertz's method can be used to find the equalizer impedance function [Ref. 6]. Given the real part,

$$\hat{R}_{q}(\omega) = \frac{A(\omega^{2})}{B(\omega^{2})} = \frac{m_{1}m_{2}-n_{1}n_{2}}{n_{2}^{2}-n_{2}^{2}}\Big|_{s=j\omega}$$
(12)

our objective is to determine the impedance

$$Z_q(s) = \frac{P(s)}{Q(s)} = \frac{m_1 + n_1}{m_2 + n_2}$$

where $s=j_{\omega}$, m_1 and m_2 are the even parts of P(s) and Q(s) respectively, and n_1 and n_2 the odd parts. The denominator polynomial, Q(s), is related to B(ω^2)

$$B(\omega^2)|_{s=i\omega} = B(-s^2) = Q(s)Q(-s)$$
 (13)

where Q(s) has all of its roots in the left hand plane and Q(-s) has its roots in the right hand plane.

We now solve for P(s), whose order must not exceed that of Q(s). Using undetermined coefficients [Ref. 6], we express $Z_q(s)$ as

$$Z_q(s) = \frac{P(s)}{Q(s)} = \frac{C_o s^{n} + C_1 s^{n-1} + \dots + C_n}{s^n + d_1 s^{n-1} + d_2 s^{n-2} + \dots + d_n}.$$
 (14)

Equating P(s) term by term to $(m_1m_2 - n_1n_2)$ and solving for coefficients yields P(s). Reference 6 discusses other procedures for the solving rational function of a driving point impedance.

4. Circuit Realization

Now that $Z_q(s)$ is known, a circuit that provides the required impedance is obtained by a conventional synthesis method. This is a procedure by which a network is generated from a given input/output relationship [Ref. 8]. The details will be discussed in the next chapter.

III. APPLICATION OF RFM

In this chapter, we will apply the mathematical procedures of the previous chapter to design a realizable circuit. As an illustration of the method, the results presented in [Ref. 1] will be duplicated and then applied to a 1-meter monopole antenna. In order for this antenna to operate in a broad frequency range, the matching network must make the antenna impedance less sensitive to frequency. This is discussed briefly in the 1-meter monopole design section.

A. EXAMPLE OF RFM APPLICATION

In order to verify a computer program (Appendix A) and to evaluate an IMSL optimization routine (Appendix B), published data generated by Carlin [Ref. 1] were used to design an equalizer network.

The matching network we wish to design for the given load is shown in Figure 2. The normalized frequency range of interest is from 0 to 1.25 (0 < ω < 1.25), and an increment of 0.25 will be used. This gives 6 break points (observation points). Since the design requirement states that the TPG must be maintained at T(0)=0.846, this forces the circuit to have a resistance value of r_o =2.29 ohms. Calculation for the DC resistance value can be obtained with the following formulas [Ref. 1]:

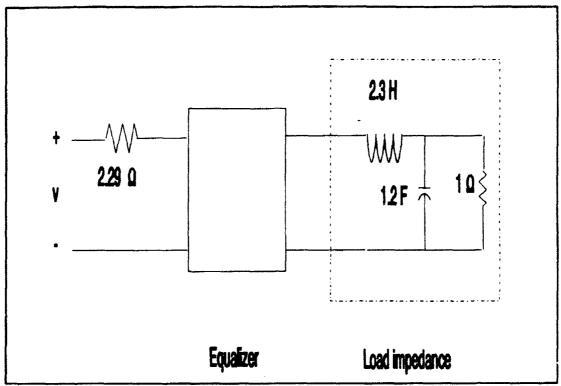


Figure 2 Given Circuit with Load

$$r_o = R_1(0) [k_o \pm \sqrt{k_o^2 - 1}]$$

 $k_o = \frac{2}{T(0)} - 1$ (15)

where T(0) is the DC gain.

Based on these formulas, there are two cases of finding the rational function: case 1 where $r_o > R_1(0)$ and case 2 where $r_o < R_1(0)$. In this example we will perform the design with case 1. With r_o known, the unknowns are no longer 5 but 4.

Keeping in mind the concept of RFM, the load impedance values are first obtained from the given RLC values shown in Figure 2. The results are given in Table I. The a_k and b_k of

equations (3) and (8) were computer programmed, a listing of which is provided in Appendix A.

Table I: Impedance of the Load

Freq	Impedance	e Value (Ω)
0.00	1.0000	+10.0000
0.25	0.9174	+j0.2998
0.50	0.7353	+10.7088
0.75	0.5525	+11.2278
1.00	0.4098	+j1.8082
1.25	0.2358	+13.0255
		-
		The second secon

Linear Combination Approximation of Equalizer Resistance

Substituting equations (2) and (6) into equation (1), the TPG is redefined in terms of $r_{\rm r}$ [Ref. 2]

$$T(\omega) = \frac{4R_{1}(\omega)\{r_{o} + \sum_{k=1}^{N} a_{k}(\omega) r_{k}\}}{\{R_{1}(\omega) + r_{o} + \sum_{k=1}^{N} a_{k}(\omega) r_{k}\} + \{X_{1}(\omega) + \sum_{k=1}^{N} b_{k}\omega\} r_{k}\}}$$

and the function to minimize is $|T_o - T(\omega)|$. Programming the above equation using an IMSL optimization subroutine ZXSSQ with $|T_o - T(\omega)|$ as a minimization function, the r_k values were obtained. The r_k values change with the initial conditions provided to the ZXSSQ subroutine. For this example, the initial values were all set to zero. These values in turn

were used to calculate the resistance and reactance at each breakpoint.

2. Rational Approximation

Now that we have represented $R_q(\omega)$ as a linear combination, the resistance values are used to calculate $\hat{R}_q(\omega)$. The function to minimize is $|\hat{R}_q - R_q|$ at the discrete frequencies ω_k , k=0,1,... n. Again, the IMSL subroutine ZXSSQ was used. The rational function is obtained as

$$R_q(\omega) = \frac{2.29}{1 + 4.8\omega^2 - 10.2\omega^4 + 8.39\omega^6} = \frac{A(\omega^2)}{B(\omega^2)}$$

A plot of the rational function and linear combination is given in Figure 3. As can be seen from the graph, the piecewise linear approximation and rational approximation are in agreement.

3. Application of Gewertz Method

We now have the real part of the equalizer impedance. From the relationship between \hat{R}_q and $\mathcal{Q}(s)$ as defined in the equations (12) through (14), we can express $B(\omega^2)$ in terms of $B(-s^2)$ as

$$B(-s^2) = 1 - 4.8s^2 - 10.2s^4 - 8.4s^6$$
.

Finding the roots of B(-s²) and writing Q(s) in factored form, we obtain Q(s) as

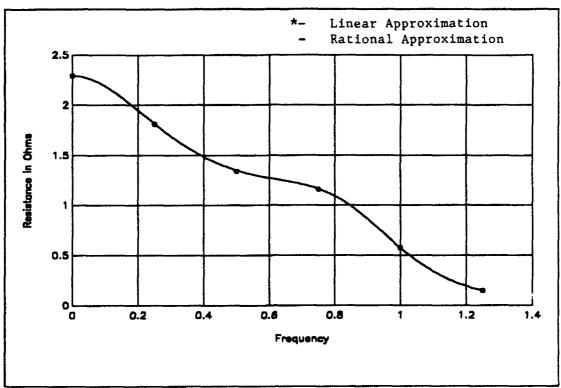


Figure 3 Rational and Linear Resistive Curves

$$Q(s) = (s+.887+j.316) (s+.887-j.316) (s+j.389) (s-j.389)$$
$$= 2.9s^3+2.9s^2+3.3s+1.$$

The roots of $B(-s^2)$ were found by a root finding IMSL subroutine called PLROC.

The next step is finding the coefficients of P(s). The equalizer impedance, $Z_q(s)$, defined in terms of P(s) and $\mathcal{Q}(s)$ is

$$Z_q(s) = \frac{P(s)}{Q(s)} = \frac{C_o s^3 + C_1 s^2 + C_2 s + C_3}{2.86 s^3 + 2.86 s^2 + 3.27 s + 1}$$

Equating the real part of $Z_q(s) \mid_{s=j\omega}$ to $\hat{R}_q(\omega)$, we have

$$m_2 m_1 - n_1 n_2 = (c_1 s^2 + c_3) (2.86 s^2 + 1) - (c_0 s^3 + c_2 s) (2.86 s^3 + 3.29 s) |_{s = j\omega}$$

$$= 2.29.$$

Equating the coefficients of like powers on both sides, we get

$$-2.86c_{o}s^{6}|_{s=j\omega} = 0 3.27c_{o}-2.86c_{2}s^{4}+2.86c_{1}s^{4}|_{s=j\omega}=0$$

$$c_{1}s^{2}+2.86c_{3}-3.27c_{2}|_{s=j\omega}=0 c_{3}=2.29.$$

Solving the above equations, we obtain $Z_{\sigma}(s)$ as

$$Z_q(s) = \frac{2.89s^2 + 2.89s + 2.29}{2.86s^3 + 2.86s^2 + 3.27s + 1}.$$

4. Circuit Realization

From $Z_q(s)$, it is necessary to find the circuit elements required to realize the matching network. For this example, the degree of the polynomial in the denominator is larger than that of the numerator. In order to divide a smaller degree into a larger degree, we will convert $Z_q(s)$ to $Y_q(s)$,

$$Y_q(s) = \frac{1}{Z_q(s)} = \frac{2.86s^3 + 2.86s^2 + 3.27s + 1}{2.89s^2 + 2.89s + 2.29}$$

The division process is as follows:

$$\begin{array}{r}
0.99s \\
2.89s^2 + 2.89s + 2.29 \overline{\smash)2.86s^3 + 2.86s^2 + 3.27s + 1} \\
\underline{2.86s^3 + 2.86s^2 + 2.27s} \\
1.00s + 1.
\end{array}$$

The first circuit element is a capacitor. Again converting and repeating the process gives

$$\begin{array}{r}
2.89s \\
1.0s+1 \overline{\smash)2.89s^2+2.89s+2.29} \\
\underline{2.89s^2+2.89s+0.00} \\
2.29
\end{array}$$

and the second element is an inductor. This process is continued until it is complete and further division cannot be carried out. The last division gives us

which is another capacitor. The remaining value is the DC resistance which equals to the original value we have calculated based on the assumed TPG of 0.846.

Now that we have our circuit elements, the question is how these elements are positioned. The crucial step is placing the first element, for other elements follow in an alternating sequence of parallel or series arms away from the load. This provides a ladder network. The final circuit to achieve $Z_q(s)$ is shown in Figure 4.

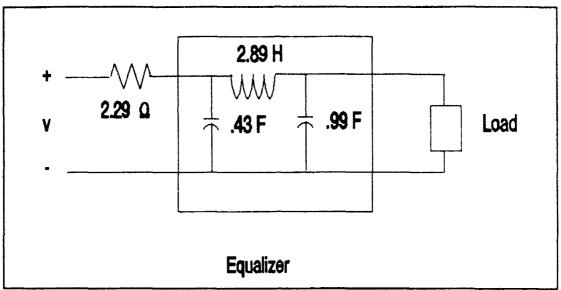


Figure 4 Final Matching Network

B. MATCHING OF 1-METER MONOPOLE ANTENNA

We have gone through an example of how a matching network is designed. We will apply this procedure to a 1-meter monopole antenna operating over 30-90 MHz with the break points chosen at 10 MHz increments. The break points are normalized to 90 MHz. Details of the calculation as shown in the previous section will be avoided, and only the highlights will be presented.

1. Wide-banding 1-meter Monopole Antenna

An antenna is defined as broadband "when its impedance and pattern do not change significantly over about an octave or more", or when the ratio between the upper frequency and the lower frequency is greater than 2 [Ref. 9].

The input impedance is highly dependent on the frequency of operation.

antenna to operate over a broad frequency range without continuous fluctuation in impedance (which in turn restricts the power transfer from the generator to the antenna), the antenna must be made lossy; i.e., a resistive load (or loads) must be added Figure Divided to the antenna [Ref. 9]. The

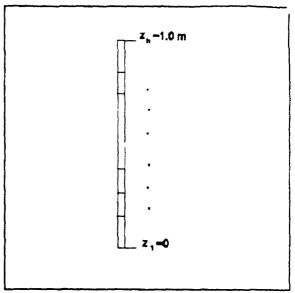


Figure 5 Monopole Antenna Divided into N segment

antenna we wish to look at has a height of 1 meter and a radius of 0.005 meter. It must operate in a frequency range of 30-90 MHz. Since the wavelength near the low frequency end is much larger than its length, the antenna is considered electrically small.

In order to calculate the resistive values to make the 1-meter monopole broadband, we used the concept of resistive loading proposed by Wu and King in [Ref. 11]. They used a continuously distributed load of the form

$$Z^{i}(z) = \frac{60\psi}{h - |z|}, \tag{16}$$

where h is the height of an antenna, and z is an incremental distance from one end point of an antenna (z=0) to the opposite end (z=h) as shown in Figure 5.

The quantity ψ is

$$\psi = 2 \left(\sinh^{-1} \left(\frac{h}{a} \right) - C(2A, 2kh) - jS(2A, 2kh) + \frac{j}{kh} \left(1 - e^{-j(2kh)} \right) \right)$$
 (17)

where a is the radius, A=ka, and k is the wavenumber in free space $(k = \omega \sqrt{\varepsilon_o \mu_o})$. The quantities C(a,x) and S(a,x) of equation (17) are defined as [Ref. 11]

$$C(a,x) = \int_{0}^{x} \frac{1-\cos W}{W} du$$
 (18)

$$S(a,x) = \int_{0}^{x} \frac{\sin W}{W} du$$
 (19)

where

$$W = (u^2 + a^2)^{1/2}. (20)$$

We have calculated the various parameters for a continuously distributed load at the geometric mean frequency of 52 MHz. For the 1-meter monopole, \mathbb{T} is [Ref. 13]

$$\psi = 2 \begin{bmatrix} \sinh^{-1}(200) - C(0.0109, 2.176) - jS(0.0109, 2.176) \\ + \frac{j}{1.088} (1 - e^{j(-2.176)}) \end{bmatrix}$$

$$= 9.24 - j1.92.$$

Referring back to equation (16), our continuous load value using a 30% multiplication factor is [Ref. 13]

$$Z^{i}(z) = \frac{15(11.4-j2.6)}{(h-z)}$$
.

Since we are interested in lumped loading, we obtained a discrete approximation to the continuous profile over a segment Δz , where N is the total number of segments $(=h/\Delta z)$ and $n\Delta z$ is the location of Z_n . We have used N=8 for the 1-meter monopole.

Once the required load values were calculated for each segment, the WIRE program [Ref. 14] was used to generate the impedance characteristics of the antenna. Table II shows the impedance characteristic of the antenna with and without the load added. The antenna impedance characteristics plotted on a Smith chart are shown in Figure 6.

Table II: Unloaded and Loaded Impedance for 1-meter Monopole Antenna

Freq (MHz)	· · · · · · · · · · · · · · · · · · ·				
(30)	(82.57	- 1375.4)	(3.850	-j346.2)	
(40)	(90.22	-1259.5)	(7.040	-1223.4	
(50)	(100.9	- 1185.0)	(12.75	-1138.4	
(60)	(115.1	-1132.5)	(20.85	-170.40)	
(70)	(132.9	-194.32)	(33.35	-19.050	
(80)	(154.1	-167.81)	(53.30	+ 151.00)	
(90)	(177.5	-152.43)	(86.90	+1115.0	

2. Equalizer Impedance Calculation

Again the same procedure as above was used to calculate the impedance. Here we varied the DC transducer gain until the resistance values just approach zero from

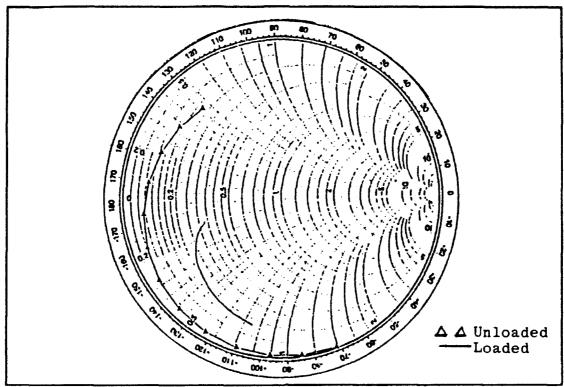


Figure 6 Impedance Characteristics of 1-meter Monopole

positive values. The corresponding gain is then treated as optimum. The same program used to find the resistance values for the previous example was used in this case after slight modification. The difference is that the design called for a fixed TPG of 0.846 for the previous case, whereas, here we are interested in the optimum TPG. An optimum TPG, To, was located at 0.4785, and the comparison of the resistance plots is given in Figure 7. The plot shows that the rational and linear approximations closely follow each other.

The rational resistance function for the monopole is

$$R_q(\omega) = \frac{3.59\omega^2}{1-8.59\omega^2+56.64\omega^4-95.01\omega^6+77.03\omega^8} = \frac{A(\omega^2)}{B(\omega^2)}.$$

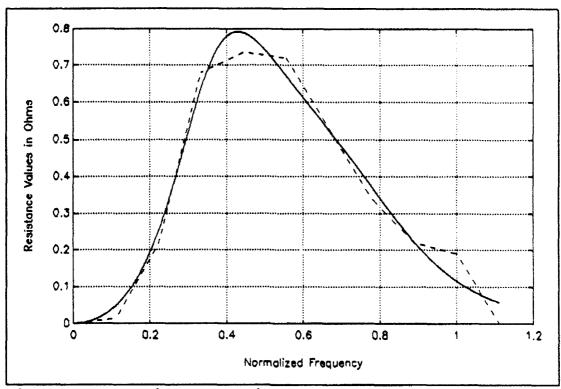


Figure 7 Comparison of Resistance Characteristic of 1 meter Monopole Antenna

Following the steps specified in the previous chapter, the positive real roots of $B(-s^2)$ are

$$(s + 0.3147 + j0.7979)$$

 $(s + 0.3147 - j0.7979)$
 $(s + 0.1947 + j0.3420)$
 $(s + 0.1947 - j0.3420)$

which gives Q(s) as

$$Q(s) = s^4 + 1.02s^3 + 1.14s^2 + 0.384s + 0.114$$
.

To be consistent with the assumed form of $B(\omega^2)$, Q(s) must be divided by a constant value such that the term independent of s is equal to 1. For the above equation, we divided by 0.114 to obtain the new Q(s) as

$$Q(s) = 8.78s^4 + 8.94s^3 + 9.97s^2 + 3.37s + 1.$$

The impedance $Z_a(s)$ is now assumed to be of the form

$$Z_{q}(s) = \frac{C_{o}s^{4} + C_{1}s^{3} + C_{2}s^{2} + C_{3}s + C_{4}}{8.78s^{4} + 8.94s^{3} + 9.97s^{2} + 3.37s + 1} = \frac{P(s)}{Q(s)}$$
$$= \frac{m_{1} + n_{1}}{m_{2} + n_{2}}.$$

The unknowns in the numerator can be obtained by multiplying the odd and even parts and subtracting

$$m_1 m_2 - n_1 n_1 = \left\{ (8.78s^4 + 9.97s^2 + 1) \left(c_o s^4 + c_2 s^2 + c_4 \right) \right\}$$

$$- (8.94s^3 + 3.37s) \left(c_1 s^3 + c_3 s \right)$$

The result is equated to $A(\omega^2)$ for $s=j\omega$. Expressing the unknown coefficients into a matrix form $\{AX\}=\{B\}$ and solving for $\{X\}$, where $\{X\}$ represents the coefficients of P(s), we have

$$\begin{bmatrix} 1.00 & 0.00 & 0.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & -8.78 & 8.94 & 0.00 \\ 0.00 & -8.94 & 9.97 & -3.37 & 0.00 \\ 0.00 & 3.34 & -1.00 & 0.00 & 0.00 \\ 0.00 & 0.00 & 0.00 & 0.00 & 8.78 \end{bmatrix} \begin{bmatrix} C_4 \\ C_3 \\ C_2 \\ C_1 \\ C_o \end{bmatrix} = \begin{bmatrix} 0.00 \\ 0.00 \\ 0.00 \\ 3.59 \\ 0.00 \end{bmatrix}.$$

The IMSL subroutine LEQIF is used to solve the matrix equation, the coefficients are found to be

$$c_0=0.0$$
 $c_1=2.33$ $c_2=2.38$ $c_3=1.77$ $c_4=0.0$

and $Z_q(s)$

$$Z_q(s) = \frac{2.33s^3 + 2.38s^2 + 1.77}{8.78S^4 + 8.94s^3 + 9.97s^2 + 3.37s + 1}.$$

In the above equation, frequency has been normalized such that s=1 corresponds to 90 MHz. Furthermore, the impedance itself is normalized such that $Z_{\alpha}=1.0$ corresponds to 500 ohms.

The matching circuit is now obtained by the synthesis method. Since the power of the denominator is larger than the numerator, we convert $Z_q(s)$ to $Y_q(s)$ and reduce the equation to

$$Y_q(s) = 3.77s + \frac{1}{0.71s + \frac{1}{3.26s + \frac{1}{1.10s} + \frac{1}{0.299}}}$$

To obtain the value of the circuit elements, they need to be denormalized. If we were to match this to a simple 75 ohm coaxial transmission line, a transformer could be used. Taking the denormalized resistance value to be 150 ohms (0.299x500) from the above equation, and using the transformer with a turns ratio of 1: 1.41, the circuit in Figure 8 is obtained.

The TPG with the matching network is plotted in Figure 9. The equalizer tunes the resistance and the reactance values of the load and maintains an approximate gain of 0.4785.

The resistance function indirectly determines the number of circuit elements required to design a matching network. From equation (10), it is seen that the maximum

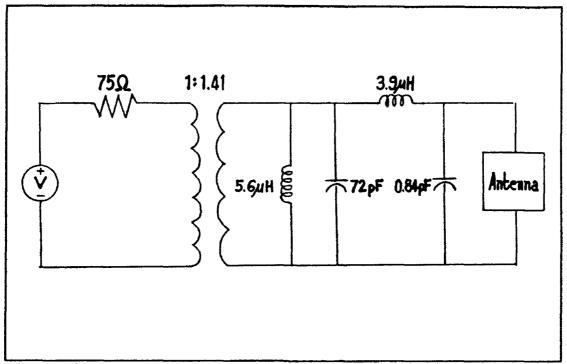


Figure 8 Matching Network for 1-meter Monopole Antenna

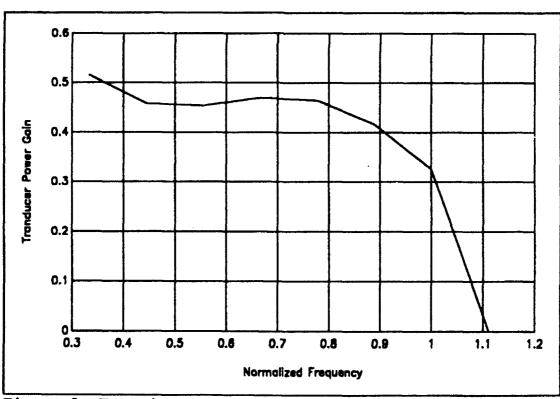


Figure 9 Transducer Power Gain

power of the denominator is 2n. The number of circuit elements required for the design is usually greater than or equal to n. Therefore, increasing the degree of denominator will increase the number of circuit elements.

Regardless of what the highest degree of the denominator polynomial is, the resistance of the rational function approximation must closely follow the linear approximation. Some of the higher order approximations with n=5 and n=6 for the 1-meter monopole are shown in Figure 10. It can be seen from the figure that as more terms are included in the polynomial a closer approximation is achieved; however, the TPG is not significantly affected by the highest power of the rational resistance function beyond a certain number of terms. Therefore, the minimum acceptable order in the rational resistance polynomial should be used. Otherwise, the mathematics becomes cumpersome.

As an example, if we had designed a matching network using n=6, the rational resistance function would have 'een

$$\hat{R}_{q}(\omega) = \frac{1.77\omega^{2}}{1-19.3\omega^{2}+180.7\omega^{4}-733.5\omega^{6}+1500.8\omega^{8}-1425.3\omega^{10}+505.5\omega^{12}}$$

and the equalizer impedance would be

$$Z_q(s) = \frac{40.79s^5 + 33.39s^4 + 63.77s^3 + 24.51s^2 + 17.07s}{4.74s^6 + 3.88s^5 + 10.38s^4 + 5.28s^3 + 6.32s^2 + 1.54s + 1}.$$

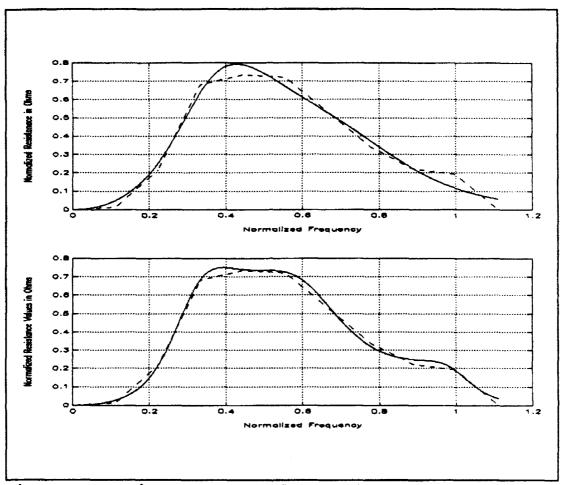


Figure 10 Resistance Curves for n=5 (top) and n=6 (bottom)

The above impedance function is realized by the network shown in Figure 11. The complexity of the matching network has been increased (compared Figures 8 and 11), but the TPG has not changed significantly. It is still given by the piecewise curve of Figure 9.

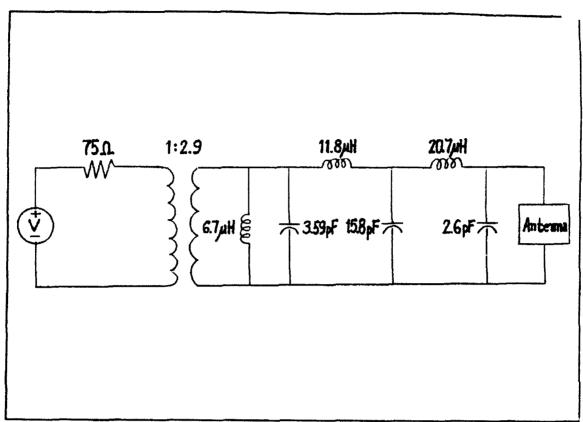


Figure 11 Matching Network for Rational Resistance Function of the Highest Power of 12 (n=6)

IV. CONCLUSION

The real frequency method provides an elegant, yet simple way of designing a matching network for any load. This thesis concentrated on using this method to design a matching network for a 1-meter monopole antenna. It can be seen from the verification of Carlin's data and from the application to a 1meter monopole antenna that this numerical technique is readily realizable and easy to implement. The basic assumption is that the antenna impedance characteristics are known and that these characteristics are provided to the circuit designer. With the 1-meter monopole antenna we had to add a resistive load along the antenna in order to make its impedance characteristics broadband. Then we were able to design the equalizer. The key to finding the equalizer impedance is determining the resistance function, which is done using the RFM. Once this is found, the equalizer can be completely determined.

The number of elements required to design a matched circuit is normally determined by the rational resistance function as shown in equation (10). Generally, n indicates the number of circuit elements required for the design. Carlin used 2n=6 for the highest degree of the rational resistance function, and his circuit was composed of three elements. For the 1-meter monopole, 2n=8 gave a minimum of

five (transformer inclusive) circuit elements. For the higher orders (n > 6), the 1-meter monopole required seven circuit elements. The number of circuit elements required is usually greater than or equal to n. Regardless of the power of the rational resistive function, the TPG is still the same as specified by the straight line approximation. Therefore, a minimum order of power of the rational resistance function that closely follows the straight line approximation should be used. Otherwise, the mathematics become cumbersome.

For this thesis, simple software was written to calculate some of the values. The ease of the programming was due to the availability of the required software in the IMSL Math Library. Listings are included in Appendix B.

Although this thesis was limited to a simple 1-meter monopole antenna, the techniques presented herein can be adapted to design a wideband matching network for any load.

APPENDIX A

PROGRAM FOR 1-METER MONOPOLE ANTENNA

```
C
     THIS PROGRAM TAKES THE IMPEDANCE DATA OF 1 METER MONOPOLE
     ANTENNA AND CALCULATES THE RESISTANCES USING TWO METHODS:
C
C
     LINEAR COMBINATION AND RATIONAL FUNCTION. THE RATIONAL
     FUNCTION
      EXTERNAL CURSM1
      PARAMETER (M=11, N=9, XJ=(N+1)*N/2, WO=5*N+2*M+XJ)
      INTEGER IXJAC, NSIG, MAXFN, IOPT, INFER, IER
      REAL PARM(4), X(N+1), F(M), XJAC(M, N+1), XJTJ(XJ), WORK(WO),
     +EPS, DELTA, SSQ, AK(20,20), BK(20,20), W(20), Z(20,20), Y(20,20), PI,
     +AZ(20,20),BZ(20,20),CZ(20,20),AY(20,20),BY(20,20),CY(20,20),
     +RQ(20), RR, XQ(20), XX, T(20), RO. TPG
      COMPLEX IMPED(20)
      COMMON RO, IMPED, AK, BK, T, TPG
      OPEN(UNIT=1, FILE='RECURSM DAT', STATUS='OLD')
      OPEN(UNIT=2, FILE='FREQM DAT', STATUS='OLD')
      OPEN(UNIT=3, FILE='AKM DAT', STATUS='OLD')
      OPEN(UNIT=4, FILE='LOAD DAT', STATUS='OLD')
      OPEN(UNIT=8, FILE='BKM DAT', STATUS='OLD')
      OPEN(UNIT=5, FILE='RQM DAT', STATUS='OLD')
      READ (6,*) TPG
      M=11
      N=9
      IXJAC=M
      NSIG=5
      EPS=0.0
      DELTA=0.0
      MAXFN=2000
      IOPT=1
      DO 110 I=1,N
 110 X(I)=0.0
      RO=0.0
      PI = 3.412
C
      ******* CALCULATE AK(W) *********
      READ(4,*)(IMPED(I),I=1,M)
      READ(2,*)(W(I),I=1,M)
      DO 10 K=1,M
      KK=K-1
         DO 20 I=1,M
              IF (W(K) .LE. W(I)) THEN
```

```
AK(K,I) = 1.0
               ELSEIF (W(KK).LE. W(I).AND.W(I) .LE. W(K)) THEN
                   AK(K,I) = (W(I) - W(KK)) / (W(K) - W(KK))
               ELSEIF (W(I) .LE. W(KK)) THEN
                   AK(K,I)=0.0
               ELSE
                   AK(K,I)=0.0
               ENDIF
      WRITE(3,*)AK(K,I)
 20
         CONTINUE
 10
      CONTINUE
C
      ********* CALCULATE BK(W) ************
      DO 50 K=1,M
         DO 51 I=1, M
         Z(K,I) = 0.0
         Y(K,I) = 0.0
         AZ(K,I) = 0.0
         BZ(K,I) = 0.0
         CZ(K,I)=0.0
         AY(K,I)=0.0
         BY(K, I) = 0.0
         CY(K,I)=0.0
         BK(K,I)=0.0
 51
         CONTINUE
 50
      CONTINUE
      DO 30 K=1,M
         DO 31 I=1,M
         IF (W(K) .LT. .001 .OR. W(I) .LT. .001) THEN
         Z(K,I)=0.0
         GO TO 32
         ENDIF
         IF (W(I) .EQ. W(K)) THEN
         BZ(K, I) = 0.0
         \lambda Z(K,I) = (W(I)/W(K) +1) *LOG(W(I)/W(K) +1)
         CZ(K,I)=W(I)/W(K)*LOG(W(I)/W(K))
         Z(K,I)=W(K)*(AZ(K,I) + BZ(K,I) - 2*CZ(K,I))
         GO TO 32
         ENDIF
         AZ(K,I) = (W(I)/W(K) +1) *LOG(W(I)/W(K) +1)
         BZ(K,I) = (W(I)/W(K)-1) * LOG(ABS(W(I)/W(K)-1))
         CZ(K,I)=W(I)/W(K)*LOG(W(I)/W(K))
         Z(K,I)=W(K)*(AZ(K,I) + BZ(K,I) - 2*CZ(K,I))
32
      KK=K-1
         IF (KK .EQ. 0.0) THEN
         BK(K,I)=Z(K,I)
         WRITE(8,*)BK(K,I)
         GO TO 31
         ENDIF
```

```
IF (W(KK) .LT. .001 .OR. W(I) .LT. .001) THEN
         Y(KK,I)=0.0
         BK(K,I)=1/((W(K)-W(KK))*PI)*(Z(K,I)-Y(KK,I),
         WRITE(8, *)BK(K, I)
         GO TO 31
         ENDIF
         IF (W(I) .EQ. W(KK)) THEN
         BY(KK,I)=0.0
         AY(KK,I) = (W(I)/W(KK)+1) *LOG(W(I)/W(KK)+1)
         CY(KK,I)=W(I)/W(KK)*LOG(W(I)/W(KK))
         Y(KK,I)=W(KK)*(AY(KK,I)+BY(KK,I)-2*CY(KK,I))
         BK(K,I)=1/((W(K)-W(KK))*PI)*(Z(K,I)-Y(KK,I))
         WRITE(8,*)BK(K,I)
         GO TO 31
         ENDIF
         AY(KK,I) = (W(I)/W(KK)+1) *LOG(W(I)/W(KK)+1)
         BY(KK,I) = (W(I)/W(KK)-1) *LOG(ABS(W(I)/W(KK)-1))
         CY(KK,I)=W(I)/W(KK)*LOG(W(I)/W(KK))
         Y(KK,I)=W(KK)*(AY(KK,I)+BY(KK,I)-2*CY(KK,I))
         BK(K,I)=1/((W(K)-W(KK))*PI)*(Z(K,I)-Y(KK,I))
         WRITE(8,*)BK(K,I)
 31
         CONTINUE
 30
      CONTINUE
      ***********************************
C
      CALL ZXSSQ(CURSM1,M,N,NSIG,EPS,DELTA,MAXFN,IOPT,PARM,X,SSQ,F,
     +XJAC, IXJAC, XJTJ, WORK, INFER, IER)
      X(10) = -(X(1) + X(2) + X(3) + X(4) + X(5) + X(6) + X(7) + X(8) + X(9))
      WRITE(1,*)'X(10)',X(10)
      WRITE(1,*)'T',T
C
      ******** CALCULATE RQ AND XQ *********
      DO 300 I=1, M
      RQ(I) = 0.0
 300
      CONTINUE
      DO 80 I=1,M
         RR=0.0
         DO 81 K=1,N+1
              KK=K+1
              RR = AK(KK, I) *X(K) + RR
 81
      CONTINUE
      RQ(I) = RO + RR
      WRITE(5,*)RQ(I)
      WRITE(1,*)'RQ(I)',RQ(I)
 80
      CONTINUE
      DO 301 I=1,M
```

```
XQ(I) = 0.0
 301
      CONTINUE
      DO 90 I=1,M
         XX=0.0
         DO 91 K=1,N+1
         KK=K+1
         XX=BK(KK,I)*X(K)+XX
 91
      CONTINUE
      XQ(I)=XX
      WRITE(1,*)'XQ(I)',XQ(I)
 90
      CONTINUE
      WRITE(1,*)'X',X
      WRITE(1,*)'SSQ',SSQ
      END
THIS IS A CALLING SUBROUTINE TO IMSL SUBROUTINE ZXSSQ.
                                                                IT
C
      WILL PROVIDE THE LINEAR RESISTANCE VALUES
C
      SUBROUTINE CURSM1 (R, M, N, F)
      INTEGER M, N, I, K, N6, J
      REAL R(N), F(M), SUM(20), AK(20,20), BK(20,20), T(20), W(20),
     +TT(20),RX(20),TPG
      COMPLEX IMPED(20)
      COMMON RO, IMPED, AK, BK, T, TPG
      N6 = N + 1
      RX(N6) = RO
      DO 10 J=1,N
      RX(J) = R(J)
 10
      RX(N6) = (RX(N6) + R(J))
      RX(N6) = -RX(N6)
      DO 100 I=1,M
      SUMA=0.0
      SUMB=0.0
         DO 15 K=1,N6
              KK=K+1
              SUM(I) = AK(KK, I) *RX(K)
              SUMA=SUMA+SUM(I)
              SUM(I) = BK(KK, I) *RX(K)
              SUMB=SUMB+SUM(I)
 15
         CONTINUE
      TT(I) = 4 * REAL(IMPED(I)) * (RO+SUMA)
      W(I) = (REAL(IMPED(I)) + SUMA + RO) **2 + (AIMAG(IMPED(I)) + SUMB) **2
      IF (W(I) .EQ. 0.0) THEN
      T(I) = 0.0
```

```
GO TO 100
      ENDIF
      T(I) = TT(I)/W(I)
 100
     CONTINUE
      DO 200 I=1,M
      F(I) = TPG - T(I)
200
     CONTINUE
      RETURN
      END
C
      THIS PROGRAM DETERMINES THE RATIONAL FUNCTION OF REISTIVE
C
C
      VALUES.
      EXTERNAL EXAMP1
      INTEGER M, N, IXJAC, NSIG, MAXFN, IOPT, INFER, IER,
     +I,J,K,L,NK,KK
     REAL PARM(4), X(9), F(11), XJAC(11,9), XJTJ(45), WORK(120), EPS,
     +DELTA, SSQ, W(20), B(20), RQ(20), RX(20), A(1)
      COMMON RQ, RX, W
      OPEN(UNIT=1, FILE='RQM DAT', STATUS='OLD')
      OPEN(UNIT=2, FILE='FREQM DAT', STATUS='OLD')
      OPEN(UNIT=3, FILE='RAT DAT B', STATUS='OLD')
     M=11
      N=9
      IXJAC=M
      NSIG=3
      EPS=0.0
      MAXFN=1000
      IOPT=1
      DELTA=0.0
      DO 10 I=1,N
 10
     X(I) = 1.0
      READ(1,*)(RQ(I),I=1,M)
      READ(2, *)(W(I), I=1, M)
           XSSQ(EXAMP1,M,N,NSIG,EPS,DELTA,MAXFN,IOPT,PARM,X,SSQ,F,
           FXJAC, IXJAC, XJTJ, WORK, INFER, IER)
       L=(N-1)/2
       A(1) = X(1)
       B(1)=X(2)**2+2*(X(3))
       WRITE(3,*)'A(1)',A(1),'B(1)',B(1)
       DO 20 I=3,L
```

```
SUM=0.0
         K=I
         PRINT *,K
         DO 30 J=3,K
               SUM=SUM+X(J-1)*X(2*K-J+1)
      CONTINUE
 30
         B(I)=X(I)**2 + (2*(X(2*K-1) + SUM))
      WRITE(3,*)'B(I)',B(I)
 20
      CONTINUE
      B(4) = X(N) **2
      WRITE(3,*)'B(4)',B(4)
      WRITE(3,*)'X',X
      WRITE(3,*)'SSQ',SSQ
      WRITE(3,*)'RQ',RQ
      WRITE(3,*)'RX',RX
      END
     ******* CALLING SUBROUTINE FOR RATIONAL FUNCTION *******
C
      SUBROUTINE EXAMP1 (X, M, N, F)
      INTEGER M, N, I, J
      REAL X(N), F(M), SUMA, SUMB, SUMC, RX(20), RQ(20), W(20)
      COMMON RQ,RX,W
      DO 10 I=1,M
      SUMA=0.0
      SUMB=0.0
      SUMC=0.0
         DO 5 J=1, N-1
         SUMA = SUMA + (X(J) **2) * (W(I) **2)
 5
         SUMA=(X(1)**2)*(W(I)**2)
         DO 6 J=2.N
         SUMB=SUMB+X(J)*(W(I)**(J-1))
         SUMC=SUMC+X(J)*((-W(I))**(J-1))
 6
      RX(I) = SUMA/(.5*(((1+SUMB)**2)+((1+SUMC)**2)))
      CONTINUE
 10
      DO 40 I=1,M
      F(I) = ABS(RX(I) - RQ(I))
      CONTINUE
 40
      RETURN
      END
```

APPENDIX B IMSL SUBROUTINE

FILE: ZXSSQ PORTRAN A

```
IMSL ROUTINE NAME
                                                                                                                                                                                                     - ZXSSQ
COMPUTER
                                                                                                                                                                                                      - TBMZSINGLE
                                                                                                                                                                                                    - NOVEMBER 1. 1984
                                LATEST REVISION
                                                                                                                                                                                                      - MINIMUM OF THE SUM OF SQUARES OF M FUNCTIONS
IN N VARIABLES USING A FINITE DIPPERENCE
LEVENEEBG-MARQUARDT ALGORITHM
                                PURPOSE
                                                                                                                                                                                                                                        LL ZXSSO(PUNC, M.N. NSIG, EPS, DELTA, HAXFN, IOPT, PARM, X, SSQ, P, XJAC, IXJAC, XJTJ, HGRK, IHFER, IEL)
                               USAGE
                                                                                                                                                                                                       - CALL
                                                                                                                                                                                                   - A USER SUPPLIED SUBFOUTINE WHICH CALCULATES
THE RESIDUAL VECTOR P(1), F(2), ..., P(n) FOR
GIVEN PARAMETER VALUES X(1), X(2), ..., X(N).
THE CALLING SEQUENCE HAS THE FOLLOWING FORM
CALL FUNC(X, N, P, P)
WHERE X IS A VECTOR OF LENGTH N AND F IS
A VECTOR OF LENGTH N.
PUNC HUST APPEAR IN AN EXTERNAL STATEMENT
IN THE CALLING PROGRAM.
FUNC MUST NOT ALTER THE VALUES OF
X(I), I=1, ..., N, H, OR N.
THE NUMBER OF RESIDUALS OR CESERVATIONS
(INPUT)
                                ARGUMENTS
                                                                                                                                             PHAC
                                                                                                                                                                                                             FUNC HUST NOT ALTER THE VALUES OF

THE NUMBER OF RESENVATIONS

ZYSSO 2500

THE NUMBER OF DESIDALS OR CESEVATIONS

ZYSSO 2500

                                                                                                                                             M
                                                                                                                                               NS IG
                                                                                                                                              EPS
                                                                                                                                             DELTA
                                                                                                                                             MAXFN
                                                                                                                                             TOPT
                                                                                                                                             PARM
```

```
INCORRECTLY.

IER=132 IMPLIES THAT APTER A SUCCESSFUL RECOVERY FROM A SINGULAR JACOBIAN, THE VECTGE X HAS CYCLED BACK TO THE FIRST SINGULARITY.

IER=133 IMPLIES THAT HAXPN WAS EXCEEDED.

WARNING ERROR

IER=38 IMPLIES THAT THE JACOBIAN IS ZERC.

THE SOLUTION X IS A STATIONARY POINT.

IER=39 IMPLIES THAT THE MARQUARDT PARAMETER EXCEEDED PARM (3). THIS USUALLY HEANS THAT THE REQUESTED ACCURACY WAS NOT ACHIEVED.
                                                                                                                                                                                                                                                                                                                      SINGLE AND DOUBLE/R32
SINGLE/H36, H48, H60
                PRECISION/HARDWARE
                 REQD. INSL ROUTINES - LEGTIP, LODECP, LUELAP, UERSET, UERTST, UGETIO
                                                                                                       - INFORMATION ON SPECIAL NOTATION AND CONVENTIONS IS AVAILABLE IN THE MANUAL INTRODUCTION OR THROUGH INSL ROUTINE UHELP
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                                                                                                       (FUNC, M. N. NSIG, EPS, DELTA, MAXPN, IOPT, PARM, X, SSQ, F, XJAC, IXJAC, XJTJ, WORK, IMPER, IER)

SPECIFICATIONS FOR ARGUMENTS

M. N. NSIG, MAXPN, IOPT, IXJAC, INPER, IER

EPS, DELTA, PARM (1), X (N), SSQ, F (M), XJAC (1),

XJTJ (1), WORK (1)

XJAC USED INTERNALLY IN PACKED FORM

SPECIFICATIONS FOR LOCAL VARIABLES

IMJC, IGRAD1, IGRAD1, IGRADU, IDELX1, IDELXL,
IDELXU, ISCALL, ISCALL, IXNEW1, IXNEW1,
IXBAD1, IFP11, IFP1, IFPU, IFPU, IFHL, IEVAL,
IXBAD1, ISW, ITER, J, IJAC, I, K, L, IS, JS, LI, LJ, ICOUNT,
IZERO, IEVEL, IEVOLD

AL, CONS2, DHORM, DSQ,
ERL2, ERL2X, PO, FOSQ, FOSQS4, G, HALF,
HH, ONE, ONEP10, CNEP5, CNESFO, AX,
HH, ONE, ONEP10, CNEP5, CNESFO, AX,
TENTH, XDIP, XHOLD, UP, ZERO,
XDABS, RELCON, PO1, TWO, HUNTW, DELTA2

SIG/6.3/
AX/0.1/
PO1, T2NTH, HALP, ZERO, CNE, ONEP5, TWO,
TEN, HUNTW, ONEP10/0.01, 0.5, 0.0,
1., 1.5, 2., 10, 0.1, 2.2, 1.210/
ERROR CHECKS
FIRST EXECUTABLE STATEMENT
                      SUBBOUTINE ZXSSQ
C
                        INTEGER
REAL
                          INTEGER
                          REAL
                          DATA
                           DATA
                        IER = 0
LEVEL = 0
CALL UERSET (LEVEL, LEVOLD)
IF (M.LE.O.OR.M.GT.IXJAC.OR.N.LE.O.OR.ICPT.LT.O.OR.IOPT.GT.2)
GO TO 305
IMJC = IXJAC-M
IP (IOPT.NE.2) GO TO 5
IP (PARM (2) .LE.ONE.OR.PARM (1) .LE.ZERO) GO TO 305
MACHINE DEPENDENT CONSTANTS
                                                                                                                                                                                                                                                                                                                       ZXSS2100
ZXSS2110
ZXSS2120
ZXSS2130
ZXSS2140
ZXSS2150
C
                 5 PREC = TRN** (-SIG-GN2)
REL = TEN** (-SIG*HALF)
RELCON = TEN** (-NSIG)
                                                                                                                                                       WORK VECTOR IS CONCATENATION OF SCALED HESSIAN, GRADIENT, DELX, SCALE, KNEW, XBAD, F(X+DEL), F(X-DEL)
```

```
FILE: ZXSSQ FORTRAN A
                                                                                           IGRAD1 = ((N+1)*N)/2
IGRAD1 = IGRAD1+1
IGRAD0 = IGRAD1+1
IDELX1 = IGRAD0
IDELX1 = IGRAD0
IDELX1 = IDELX1+1
IDELX0 = IDELX1+1
ISCAL1 = IDELX0
ISCAL1 = ISCAL1+1
ISCAL0 = ISCAL1+1
ISCAL0 = ISCAL1+1
ISCAL0 = ISCAL1+1
ISCAL0 = IXNEW1+1
IXNEW1 = IXNEW1+1
IXBAD1 = IXNEW1+1
IXBAD1 = IXBAD1+N
IPPL1 = IPPL1+M
IPPL1 = IPPL1+M
IPPU = IFPL1+M
IPPU = IFPL1+M
IPPL1 = IFPL1+1
IXBAD1 = IXDAD1+N
IXPD0 = IXBAD1+N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           INJC = IXJAC - M

AL = ONE
CONS2 = TENTH
IF (IOPT.EQ.0) GO TO 20
IP (IOPT.EQ.1) GO TO 10
AL = PARM (1)
PO = PARM (2)
UP = PARM (3)
CONS2 = PARM (4)
GO TO 15

10 AL = PO 1
PO = THO
UP = HUNTW
15 ONESPO = ONE/FO
FOSO = FO*FO
FOSO = FO*FO
FOSO = FO*FO
FOSO = ONE/FO
FOSO = ONE/FO
FOSO = ONE/FO
FOSO = FO*FO

                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               INITIALIZE VARIABLES
\boldsymbol{c}
  ٤,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               MAIN LOGP
                                                  30 \text{ SSQOLD} = SSQ
                                                                                               CALCULATE JACOBIAN

IF (INFER.GT.O.OR.IJAC.GE.N.OR.IOPT.EQ.O.OR.ICOUNT.GT.D) GO TO 55

RANK ONE UPDATE TO JACOBIAN
    C
                                                                                               IJAC = IJAC+1
                                          IJAC = IJAC+1
DSQ = ZERO
DO 35 J=IDELXL, IDELXU
DSQ = DSQ+WORK (J) *WORK (J)

35 CONTINUE
IF (DSQ.LE.ZERO) GO TO 55
DO 50 I=1, M
G = F(1) -WORK (IFML1+I)
K = I
DO 40 J=IDELXL, IDELXU
G = G+XJAC (K) *WORK (J)
K = K+IXJAC
CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ZXSS2750
ZXSS2760
ZXSS2780
ZXSS22780
ZXSS22810
ZXSS2810
ZXSS28820
ZXSS28820
ZXSS28840
ZXSS28860
ZXSS28860
ZXSS28860
ZXSS28860
ZXSS28860
ZXSS28860
                                                40
                                                                                                                                                CONTINUE
                                                                                                                                            G = G/DSQ

K = I

DO 45 J=IDELXL, IDELXU

XJAC(K) = XJAC(K) -G*WORK(J)

K = K*IXJAC
                                                                                                                                                CONTINUE
                                                    Số CONTINUÊ
GO TO BÔ
```

```
ZXSS2890
ZXSS2900
ZXSS2910
ZXSS2920
ZXSS2930
                 JA

K = -IMJC

DO 75 J=1, N

K = K+IMJC

YDABS = ABS(X(J))

HH = REL*(AMAX1(XDABS,AX))

XHOLD = X(J)

X(J) = X(J)+HH

CALL FUNC (X, M, N, WORK (IFPL))

IEVAL = IEVAL+1

X(J) = XHOLD

IF (ISW.EQ.1) GO TO 65

CE
                                                                                                                                                                                                                                            JACOPIAN BY INCREMENTING X
                                                         X(J) = XHOLD-HH
CALL PUNC (X, M, N, WORK (IFHL))
IFFAL = IEVAL+ 1
X(J) = XHOLD
RHH = HALF/IIH
DO 60 I=IFPL, IFPU

X = K+1
XJAC(K) = (WORK (I) - WORK (I+M)) *RHIII
CONTINUE
GO TO 75
                                                                                                                                                                                                                                          CENTRAL DIFFERENCES
C
                    60
                                                                                                                                                                                                                                             FORWARD DIFFERENCES
С
                  65 RHH = ONE/HH
DO 70 I=1, M
K = K+1
XJAC(K) = (WORK(IFPL1+I)-P(I)) *RHH
70 CONTINUE
75 CONTINUE
                  ## CONTINUE

## ERL2X = ERL2

## ERL2 = ZERO

## ERL2 = ZERO

## ERL2 = ZERO

## ERL2 = ZERO

## ERL2 = ERL2

## ERL2 = ERL2

## ERL2 = ERL2 =
                                                                                                                                                                                                                                           CALCULATE GRADIENT
                                                                                                                                                                                                                                           CONVERGENCE TEST POR NORM OF GRADIENTZXSS3350
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       C
                                          IP (IJAC.GT.O) GO TO 95
IP (ERL2.LE.DELTA2) INFER = INFER+4
IP (ERL2.LE.CONS2) ISW = 2
                                                                                                                                                                                                                                            CALCULATE THE LOWER SUPER TRIANGE OF JACOBIAN (THANSPOSED) * JACOBIAN
              95 L = 0
IS = -IXJAC
DO 110 I=1, N
IS = IS+IXJAC
JS = -IXJAC
DO 105 J=1, I
JS = JS+IXJAC
L = L+1
SUM = ZERO
DO 160 K=1, M
LI = IS+K
LJ = JS+K
SUM = SUM+XJAC(LI) *XJAC(LJ)

105 CONTINUE
105 CONTINUE
107 CONTINUE
108 CONVERGE
                                                                                                                                                                                                                                              CONVERGENCE CHECKS
                                           IP (INFER.GT.0) GO TO 315
IP (IEVAL.GE.MAXFN) GC TO 290
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ZXSS3600
```

```
FILE: ZXSSQ FORTRAN A
                                                                                                                                                                                        2XSS3610
2XSS3620
2XSS3630
2XSS3650
2XSS3650
4XSS3660
2XSS3670
                                                                                         COMPUTE SCALING VECTOR
               IF (IOPT.EQ.0) GO TO 120

K = 0

DO 115 J=1, N

K = K+J
     WORK (ISCAL1+J) = XJTJ(K)
115 CONTINUE
GO TO 135
                                                                                         COMPUTE SCALING VECTOR AND NORM
      120 DNORM = ZEKO
    120 DNUMM = 2EMO

K = 0

DO 125 J=1, N

K = K+J

WORK (ISC ^L 1+J) = SORT (XJTJ (K))

DNORM = DNORM+YJTJ (K) *XJTJ (K)

125 CONTINUE

DNORM = ONE/SQRT (DNORM)

NORM
                                                                                         NORMALIZE SCALING VECTOR
     DO 130 J=ISCALL, ISCALU
WORK (J) = WORK (J) * DNORM*ERI2
130 CONTINUE
     135 ICOUNT = 0
140 K = 0
140 K = 0
00 150 I=1, N
00 145 J=1, I
K = K+1
WORK (K) = XJTJ(K)
145 CONTINUE
WORK (K) = WORK (K) + WORK (ISCAL1+I) *AL
WORK (IDELX1+I) = WORK (IGRAD1+I)
150 CONTINUE
                                                                                          ADD L-M FACTOR TO DIAGONAL
                                                                                                                                                                                         2X553890
2X553890
2X553910
2X553910
2X553920
2X553940
2X553940
2X553950
    CHCLESKY DECOMPOSITION

155 CALL LEOTIP (WORK, 1, N, WORK (IDELXL), N, 0, G, XHOLD, IER)

IF (IER.EQ.O) GC TO 160

IF (IJAC.GT.O) GO TO 55

IF (IBAD.LE.O) GO TO 240

IP (IBAD.GE.2) GO TO 310

GO TO 190

160 IF (IBAD.NE.-99) IBAD = 0
    CALCULATE !

165 DO 170 J=1, N
WORK (IXNEW1+J) = X (J) -WORK (IDELX1+J)

170 CONTINUE
CALL FUNC (WORK (IXNEWL), M, N, WORK (IPPL))
IEVAL = IEVAL+1
SSQ = ZERO
DO 175 I=IPPL, IPPU
SSQ = SSQ+WORK (I) * WORK (I)

175 CONTINUE
IF (ITER.GE.O) GO TO 185
                                                                                         CALCULATE SUM OF SQUARES
                                                                                                                                                                                         ZXSS4060
ZXSS4070
ZXSS4080
                      (ÎTER.GE.O) GO TO 185
              ITER = 0

SSQCLD = SSQ

DO 180 I=1, M

F(I) = WOFK (IFPL1+I)
                                                                                         SSQ FOR INITIAL ESTIMATES OF X
     180 CONTINUE

GO TO 55

185 IF (IOPT. EQ. 3) GO TO 215
               IF (SSQ.LE.SSQCID) GO TO 205 CHECK DESCENT PROPERTY
    190 ICQUNT = ICQUNT+1

AL = AL+FOSQ

IF (IJAC.BQ.0) GO TO 195

IF (ICQUNT.GE.4.OR.AL.GT.UP) GO TC 200

195 IF (AL.LE.UP) GC TO 140

IF (IBAD.EQ.1) GO TO 310

IER = 39

GO TO 315

200 AL = AL/FOSQS4
                                                                                          INCREASE PARAMETER AND TRY AGAIN
                                                                                                                                                                                        ZXSS4280
ZXSS4290
ZXSS4300
ZXSS4310
```

```
FILE: ZXSSQ PORTGAN A
                                                                                                                                          2XSS4330
2XSS4340
2XSS4350
2XSS4360
           GO TO 55
                                                                   ADJUST MARQUARDT PARAMETER
   ADJUST MARQUAE

205 IP (ICOUNT. EQ. 0) AL = AL/F0

IP (ERL2X.LE. ZEWO) GO TO 210

G = ERL2/ERL2X

IP (ERL2.LT. ERL2X) AL = AL*AMAX1 (CNESPO, G)

IF (ERL2.GT. ERL2X) AL = AL*AMIN1 (FO, G)

210 AL = AMAX1 (AL, PREC)
                                                                                                                                          2XSS4376
2XSS4380
   ONE ITERATION CYCLE COMPLETED
   225 CONTINUE
                                                          RELATIVE CONVERGENCE TEST FOR X
   IF (AL.GT.5.0) GO TO 30

DO 230 J=1, N

XDIP = ABS(WORK(IDELX1+J))/AMAX1(ABS(X(J)),AX)

IF (XDIF.GT.RELCON) GO TO 235

230 CONTINUE
   235 SOBIF = ABS(SSQ-SSOOLD)/AMAX1(SSOOLD, AX)
IF (SQDIF.LE.EPS) INFER = INFER+2
GO 10 30
                                                                   SINGULAR DECOMPOSITION
   240 IF (IBAD) 255,245,265
                                                                   CHECK TO SEE IF CURRENT ITERATE HAS CYCLED BACK TO THE LAST SINGULAR POINT
   245 DO 250 J=1, N

XHOLD = WORK (IXBAD1+J)

IF (ABS(X(J)-XHOLD).GT.RELCOH*AMAX1(AX,ABS(XHOLD))) GO TO 255

250 CONTINUE
                                                                                                                                          2X5S4690
2X5S4700
2X5S4710
           GO 10 295
                                                                  UPDATE THE BAD X VALUES
   255 DO 260 J=1,N
NORK(IXBAD1+J) = X(J)
260 CONTINUE
IBAD = 1
                                                                   INCREASE DIAGONAL OF HESSIAN
   265 IF (IOPT.NE.0) GO TO 280

K = 0

DO 275 I=1, N

DO 270 J=1, I

K = K+1
   | K = K+1 | WORK(K) = XJTJ(K) | CONTINUE | WORK(K) = ONEP5* (XJTJ(K) + AL*ER12*WORK(ISCAL1+I)) + REL | IBAD = 2 | GO TO 155
                                                                   REPLACE ZEROES ON HESSIAN DIAGONAL
   280 IZERC = 0
DO 285 J=ISCALL, ISCALU
IF (WORK (J) .GT. ZERO) GO TO 285
IZERO = IZERG+1
WORK (J) = ONE
285 CONTINUE
IF (IZERO.LT.N) GO TO 140
IER = 38
GO TO 315
                                                                   TERMINAL ERRCR
    290 IER = IER+1
295 IER = IER+1
IEE = IER+1
305 IER = IER+1
310 IER = IER+129
                                                                                                                                          ZXSS5000
ZXSS5010
ZXSS5020
ZXSS5030
ZXSS5040
            iř (IEŘ. EQ. 130) GO TO 335
```

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PILE: ZXSSQ FORTRAN A
```

```
C

315 G = SIG

DO 320 J=1, N

XHOLD = ABS(WORK(IDELX1+J))

IF (XHOLD.LE.ZERO) GO TC 320

G = AMIN1 (G, -ALOG10(XHOLD) + ALOG10(AMAX1(AX, ABS(X(J)))))

320 CONTINUE

IF (N.GT.2) GO TO 330

DO 325 J = 1, N

325 WORK (J+5) = WORK (J+IGRAD1)

330 WORK (J) = FRL2+FRL2

WORK (Z) = IEVAL

SSO = SSOULD

WORK (Z) = IEVAL

WORK (S) = ITER

335 CALL UERSET (LEVOLD, LEVOLD)

IF (IER.EQ.O) GO TO 9005

CALL UERTST (IER, 6HZXSSQ))

RETURN

END
```

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